

DOI: 10.31319/2519-8106.1(48)2023.280697  
UDC 621.74

**Sereda Borys**<sup>1</sup>, Doctor of Technical Sciences, Professor, Head Department of automobiles and automotive industry

**Серєда Б.П.**, доктор технічних наук, професор, завідувач кафедри автомобілів та автомобільне господарство

ORCID: 0000-0002-9518-381X

e-mail: seredabp@ukr.net

**Baskevich Oleksander**<sup>2</sup>, Candidate of Physico-mathematical Sciences, Associate Professor, Senior Researcher in the Research Unit

**Баскевич О.С.** кандидат фізико-математичних наук, старший науковий співробітник НДЧ

ORCID: 0000-0002-3227-5637

**Kryhliak Irina**<sup>1</sup>, Doctor of Technical Sciences, Professor, Head Department of industrial engineering

**Кругляк І.В.**, доктор технічних наук, професор, завідувач кафедри галузевого

машинобудування

ORCID: 0000-0002-9518-381X

**Chygov Igor**<sup>3</sup>, Zaporozhye Casting-Mechanical Plant LLC, foreman of main production

**Чижов І.О.**, бригадир основного виробництва

**Bilozir Igor**<sup>1</sup>, postgraduate student of the Department of AAG

**Білозір І.В.**, аспірант кафедри ААГ

**Prolomov Anton**<sup>1</sup>, postgraduate student of the Department of AAG

**Проломов А.А.**, аспірант кафедри ААГ

<sup>1</sup>Dnipro State Technical University, Kamianske

<sup>1</sup>Дніпровський державний технічний університет, м. Кам'янське

<sup>2</sup>Ukrainian State University of Chemistry and Technology, Dnipro

<sup>2</sup>Український державний хіміко-технологічний університет, м. Дніпро

<sup>3</sup>Zaporozhye Casting-Mechanical Plant LLC, Zaporizhzhia

<sup>3</sup>ООО «Запорізький ливарно-механічний завод», м. Запоріжжя

**MATHEMATICAL MODEL OF EXPERIMENTAL METHODS FOR OBTAINING THE  
STRUCTURE FACTOR WHEN STUDYING THE INFLUENCE OF CATHODIC  
OVERVOLTAGE ON THE STRUCTURE OF ELECTRODEPOSITED  
ALLOYS NI-P, FE-P AND CO-P**

**МАТЕМАТИЧНА МОДЕЛЬ ЕКСПЕРИМЕНТАЛЬНИХ МЕТОДІВ ОТРИМАННЯ  
СТРУКТУРНОГО ФАКТОРУ ПРИ ДОСЛІДЖЕННІ ВПЛИВУ КАТОДНОЇ  
ПЕРЕНАПРУГИ НА СТРУКТУРУ ЕЛЕКТРООСАДЖЕНИХ  
СПЛАВІВ NI-P, FE-P І CO-P**

*The paper considers the diffractograms obtained during X-ray studies that have relative units, and for the study of close order, the structural factor that has electronic units is used. It is emphasized that the nonlinearity of the mathematical model necessitates the use of numerical methods and means of their computer implementation. The structure factor is obtained from experimental data by introducing various corrections that depend on the wavelength of the radiation, the geometry of the survey, the shape of the samples and their composition. Electrolyte solutions with a minimum concentration of  $\text{Na}_2\text{HPO}_2$  were used to determine the effect of pulsed current regimes on the close order of Ni-P,*

*Co-P and Fe-P alloys. To clarify the phase state of the alloys, the micro electronograms of the alloys with the maximum phosphorus content were considered. The described approach is implemented for the case of research of cathodes overvoltage on the structure of electrodeposited alloys.*

**Keywords:** *mathematical model, structure factor, diffractogram, scattering intensity, normalizing factor, structure modeling.*

*У роботі розглядається дифрактограми, що одержують під час рентгенівських досліджень мають відносні одиниці, а для дослідження близького порядку використовують структурний фактор, який має електронні одиниці. Підкреслено, що нелінійність математичної моделі зумовлює необхідність застосування чисельних методів та засобів їх комп'ютерної реалізації.*

*Структурний фактор отримують з експериментальних даних введенням різних поправок, які залежать від довжини хвилі випромінювання, геометрії зйомки, форми зразків та їх складу. У випадку нормування інтенсивності даним методом діють таким чином: знаходять відношення експериментальної інтенсивності до інтенсивності розсіяння одним атомом, тобто суму квадратів атомного фактору і комптонівського розсіяння. Якщо в експериментальну інтенсивність введені інші похибки та відсутні систематичні похибки, то отримане співвідношення при великих значення  $S$  повинно рівномірно осцилювати навколо деякого постійного числа, обернена величина якого є нормуючим множником.*

*Для визначення впливу режимів імпульсного струму на близький порядок сплавів Ni-P, Co-P і Fe-P використовували розчини електролітів з мінімальною концентрацією  $\text{Na}_2\text{HPO}_2$ . Для уточнення фазового стану сплавів розглянуто мікроелектронограми сплавів з максимальним вмістом фосфору. Описаний підхід реалізований для випадку дослідження катодної перенапруги на структуру електроосаджених сплавів Ni-P, Fe-P та Co-P використання ресурсів у залізничній сфері діяльності. Одержані результати добре узгоджуються з даними інших авторів.*

**Ключові слова:** *математична модель, структурний фактор, дифрактограма, інтенсивність розсіяння, нормуючий множник, моделювання структури.*

### Formulation of the problem

When studying diffractograms obtained during X-ray studies, they have relative units, and for the study of close order, the structure factor is used, which has electronic units. The structure factor is obtained from experimental data by introducing various corrections that depend on the wavelength of the radiation, the geometry of the survey, the shape of the samples and their composition. Monochromatization methods are based on the selective reflection of radiation with a wavelength  $\lambda$  from a number of atomic planes of a single crystal with an interplane distance  $d$  and use the Wolff-Bragg condition. When studying diffractograms obtained during X-ray studies, they have relative units, and for the study of close order, the structure factor is used, which has electronic units. The structure factor is obtained from experimental data by introducing various corrections that depend on the wavelength of the radiation, the geometry of the survey, the shape of the samples and their composition.

Monochromatization methods are based on the selective reflection of radiation with a wavelength of  $\lambda$  from a number of atomic planes of a single crystal with an interlunar distance and use the Wolff-Bragg condition. The peculiarity of this method is that it is at an angle  $2\theta$  there is a reflection of higher orders of radiation with wavelengths  $\lambda/2, \lambda/3$  etc. To obtain the structure factor, it is necessary to convert the experimental scattering intensity, which is obtained in an arbitrary scale of units, with the help of normalizing factors to electronic scattering units. As a result of modeling, the nature of the structural factor was studied, which was translated into the experimental intensity of scattering, which is obtained in an arbitrary scale of units, with the help of normalizing factors to electronic scattering units. For this purpose, the property of scattering intensity is used: when the modulus of the scattering vector increases  $S$  structure factor  $i(s)$  goes to unity ( $s \rightarrow \infty, i(\infty) = 1$ ). It was also established that during pulsed electrodepositing to achieve an amorphous state in alloys Ni-P, Co-P, Fe-P a 1—2 % lower phosphorus content is required, compared to alloys deposited using direct current.

### Analysis of recent research and publications

Diffraction patterns obtained during X-ray studies have relative units, and for the study of close order, the structure factor is used, which has electronic units. The structure factor is obtained from experimental data by introducing various corrections that depend on the wavelength of the radiation, the geometry of the survey, the shape of the samples, and their composition [1—3]. Monochromatization methods are based on the selective reflection of radiation with a wavelength of  $\lambda$  from a number of atomic planes of a single crystal with an interplane distance of  $d$  and use the Wolf-Bragg condition [4]:

$$2d \sin \theta = n\lambda, \quad (1)$$

where  $\theta$  — half the scattering angle,  $n=1,2,\dots$  — reflection order.

The peculiarity of this method is that it is at an angle  $2\theta$  there is a reflection of higher orders of radiation with wavelengths  $\lambda/2, \lambda/3$  etc. To get rid of harmonics in the registered radiation, modern methods of radio electronics allow using a discriminator to limit the energy of pulses from the upper and lower limits and select the maximum amplification factor [1—3].

For a flat sample, the absorption coefficient has the following expression [5]:

$$A(2\theta, E, E') = \frac{A_0 \sin \beta}{\mu(E) \sin \beta + \mu(E') \sin \gamma} \left\{ 1 - \exp \left[ -t \left( \frac{\mu(E)}{\sin \gamma} + \frac{\mu(E')}{\sin \beta} \right) \right] \right\}, \quad (2)$$

reflected rays and the surface of the sample, respectively;  $\mu(E)$  — absorption coefficient with energy  $E$ ,  $t$  — sample thickness, where  $A_0$  — cross section of the primary beam;  $\gamma$  and  $\beta$  — angles between incident and reflected rays.

In addition, the reflection of X-ray radiation from a single crystal is accompanied by a partial polarization of the radiation. The same polarization occurs during the scattering of radiation by the sample, therefore, a polarization correction is introduced into the experimental intensity associated with the difference in polarization conditions during scattering at different angles:

$$P(2\theta) = \frac{(1 + k \cos^2(2\theta))}{1 + k'}, \quad (3)$$

(for the focus system used  $k'=1$ ).

To obtain the structure factor, it is necessary to convert the experimental scattering intensity, which is obtained in an arbitrary scale of units, with the help of normalizing factors to electronic scattering units. For this purpose, the property of scattering intensity is used: when the modulus of the scattering vector increases  $S$  structure factor  $i(s)$  strive to one ( $s \rightarrow \infty, i(\infty) = 1$ ), but the value  $i(s)$  should be transformed in such a way that for the case when Compton scattering is registered, it would be included in the expression of the structure factor [3]:

$$i(s) = \frac{[I(s) + I_k(s)] - I_k(s)}{f^2(s)}, \quad (4)$$

where  $I_k(s)$  — intensity of compton scattering of an atom.

The first term in square brackets (4) is related to the experimental scattering intensity  $I_e(s)$  using an unknown constant multiplier  $\Lambda$ , which is the normalizing factor for the experimental scattering intensity:

$$\Lambda I_e(s) = I(s) + I_k(s). \quad (5)$$

The ratio (5) has the form:

$$i(s) = \frac{\Lambda I_e(s) - I_k(s)}{f^2(s)}. \quad (6)$$

Since, at  $s \rightarrow \infty$   $i(s) \rightarrow 1$ , then it follows the normalizing factor  $\Lambda$  should be chosen in such a way that at large values  $S$  multiplication was approaching  $\Lambda I_e(s) \rightarrow f^2(s) + I_k(s)$ . This fact is not easy to use, because significant errors are possible during experimental measurements of scattering intensity.

In the case of normalization of the intensity by this method, they act as follows: the ratio of the experimental intensity to the intensity of scattering by one atom is found, that is, the sum of the squares of the atomic factor and Compton scattering. If other errors are introduced into the experimental intensity and there are no systematic errors, then the obtained ratio at large values should oscillate evenly around some constant number, the inverse of which is the normalizing factor. Other methods of finding the normalizing factor are less effective and poorly substantiated.

Scattering intensity normalization in the case of polyatomic objects does not fundamentally differ from those considered above and can be carried out similarly, using summation by the number of components, their quantitative composition and tables of X-ray scattering factors [6].

If the normalizing factor  $\Lambda'$  determined with some error  $\Delta$  from its exact meaning  $\Lambda$  ( $\Lambda' = \Lambda + \Delta$ ), is a structural factor  $i(S) = \frac{\Lambda' I(S) - I(S)}{f^2(S)}$ , which is included in FRRA can be written as [2]:

$$i(S)_{\text{excn}} = \frac{\Lambda' \cdot I(S) - I(S)}{f^2(S)} = \frac{\Lambda' I(S) - I(S)}{f^2(S)} + \frac{\Delta \cdot I(S)}{f^2(S)}. \quad (7)$$

Then FRRA will have the form:

$$G'(r) = 4\pi\rho(r)r + \left\{ \frac{\Delta}{\Lambda} \cdot 4\pi\rho(r)r^2 + \frac{2\Delta}{\pi\Lambda} \cdot \int_0^{S_{\max}} \frac{I(S)}{f^2(S)} \cdot \sin(Sr) ds + \frac{2\Delta}{\pi\Lambda} \left[ \frac{\sin(S_m r) - S_m r \cdot \sin(S_m r)}{r^2} \right] \right\} = 4\pi\rho(r)r + \{G_1 + G_2 + G_3\}. \quad (8)$$

Influence  $G_1$  comes down to the fact that the maxima on the FRRA curve become more blurred, and the addn  $G_2$  describes oscillations that decay quickly. The main error is introduced by the third term in (8) Error  $\Delta$  in the determination of the structural factor gives maxima at small values when calculating the FRRA  $r$ . Using this statement and the results of calculations, it is possible to approach the true value of the structural factor, minimizing all errors, which means to correctly model the structure of alloys and find many physical quantities.

### Formulation of the purpose of the research

The purpose of researching the effect of cathodic overvoltage on the structure of electrodeposited Ni-P, Fe-P, and Co-P alloys is to show the possibilities of using a mathematical model of the dependence of the phase state of Ni-P, Co-P, and Fe-P alloys on pulsed current deposition modes.

### Presenting main material

Electrolyte solutions with a minimum concentration were used to determine the influence of pulsed current regimes on the close order of Ni-P, Co-P, and Fe-P alloys  $\text{Na}_2\text{HPO}_2$  in such a way that the structure of the alloys is crystalline during deposition using direct current, and amorphous during pulsed current. The samples were deposited with a pulsed current at a frequency of 30 Hz with a change in pitch from 2 to 32. The magnitude of the overvoltage on the cathode did not change for all deposition modes, but the average current density increased. At the same current density with a decrease in the split ratio from 32 to 2, the maximum value of the cathodes overvoltage dropped more than twice, regardless of the concentration  $\text{Na}_2\text{HPO}_2$  in the electrolyte solution [7—10].

Depending on the concentration  $\text{Na}_2\text{HPO}_2$  in the electrolyte solution, the resulting Ni-P, Fe-P, Co-P alloys had a microcrystalline or amorphous state [9—12]. During deposition using a direct current, the amorphous state was fixed at a sodium hypophosphite concentration of at least 10, 12, and

14 kg/m<sup>3</sup> (respectively for alloys Ni-P, Co-P and Fe-P). The use of pulsed current made it possible to reduce the concentration of sodium hypophosphite in the electrolyte solution to 8 kg/m<sup>3</sup> for Ni-P, and up to 4 kg/m<sup>3</sup> for Co-P and Fe-P. Moreover, in alloys deposited using a pulsed current, the amorphous state was fixed at a lower phosphorus content (10, 10,5, and 15 at. %) compared to films obtained using a direct current (12, 12,5, and 17 at. %). This fact is explained by the fact that the yield of metal in the current during deposition with the help of a pulsed current ( $f = 30$  Hz,  $Q = 32$ ) was no more than 45—50 %. This mode of deposition contributed to the penetration of about 1,5—2 at. % of hydrogen into the crystal lattice of the metal along with phosphorus during the amorphization of alloys based on cobalt, nickels, and iron [13—15].

It was established that the main influence on the formation of close-order amorphous alloys is caused by the amount of cathodes overvoltage [9, 10, 12]. Tabl. 1—3 show the dependences of the phase state of Ni-P, Co-P, and Fe-P alloys on pulsed current deposition modes.

Table 1. Dependence of the phase state of Ni-P alloys on deposition modes

№	Modes of deposition							P, at. %	Structure
	f, Hz	Q	j, A/m <sup>2</sup>	$\eta_{MAX}$ , V	$\eta_{RES}$ , V	V <sub>INC</sub> , V/s	V <sub>СП</sub> , V/s		
1	30	32	200	0,92	0,65	270	4,3	14	A
2	30	16	250	0,92	0,68	120	5,6	12	A+MK
3	30	8	300	0,92	0,72	50	6,4	11	MK
4	30	4	350	0,92	0,76	20	7	10	MK
5	30	2	400	0,92	0,8	7,5	7,5	8	MK

Table 2. Dependence of the phase state of Co-P alloys on deposition regimes

№	Modes of deposition							P, at. %	Structure
	F, Hz	Q	j, A/m <sup>2</sup>	$\eta_{MAX}$ , V	$\eta_{RES}$ , V	V <sub>INC</sub> , V/s	V <sub>СП</sub> , V/s		
1	30	32	200	0,92	0,65	154	4	17	A
2	30	16	250	0,92	0,68	70,3	4,35	13	A+MK
3	30	8	300	0,92	0,72	28,6	4,7	11	MK
4	30	4	350	0,92	0,76	10,8	5,15	10	MK
5	30	2	400	0,92	0,8	5,4	5,4	8	MK

Table 3. Dependence of the phase state of Fe-P alloys on deposition regimes

№	Modes of deposition							P, at. %	Structure
	f, Hz	Q	j, A/m <sup>2</sup>	$\eta_{MAX}$ , V	$\eta_{RES}$ , V	V <sub>INC</sub> , V/s	V <sub>СП</sub> , V/s		
1	30	32	200	0,92	0,65	260	4,5	17	A
2	30	16	250	0,92	0,68	190	4,6	15	A+MK
3	30	8	300	0,92	0,72	95	4,85	11	MK
4	30	4	350	0,92	0,76	23	5,2	10	MK
5	30	2	400	0,92	0,8	7,3	5,55	8	MK

In the alloy Ni<sub>86</sub>P<sub>14</sub>, despite the same maximum value of the overvoltage on the cathode (0.92 V), the residual value of the overvoltage increases from 0.65 to 0.8 V with a decrease in the gap ratio from 32 to 2, which leads to a decrease in the degree of imbalance of the crystallization process,

the rate of potential increase from 270 to 7,5 V/c, the phosphorus content and to the change in the alloy structure from amorphous to microcrystalline (tabl. 1).

Tabl. 1—3 show the following designations:  $f$  and  $Q$  — frequency and frequency of current pulses;  $j$  is the current density;  $\eta_{\text{MAX}}$  and  $\eta_{\text{RES}}$  — maximum and residual value of cathodes overvoltage;  $V_{\text{INC}}$  and  $V_{\text{CII}}$  — speed of rise and fall of cathodes overvoltage;  $P$  is the phosphorus content in the film. Structure: (A) — amorphous, (MC) — microcrystalline.

Similar results are observed for alloys  $\text{Co}_{83}\text{P}_{17}$  and  $\text{Fe}_{83}\text{P}_{17}$ , in which a decrease in sparability from 32 to 2 causes a decrease in the potential rise from 154 to 5,4 V/s and from 260 to 7,3 V/s, respectively, and this changes the structure of the alloys from amorphous to crystalline. Fig. 2.1 shows the diffractograms of the alloys  $\text{Ni}_{86}\text{P}_{14}$ ,  $\text{Ni}_{90}\text{P}_{10}$ , obtained at different pulse current regimes. As can be seen from Fig. 1 and Tabl. 1, a decrease in the rate of potential growth from 270 to 7,5 V/s leads to a change in the formed structure from amorphous to microcrystalline. Alloy composition  $\text{Ni}_{86}\text{P}_{14}$ , obtained at a potential growth rate of 270 V/s, has diffuse maxima (Fig. 1, curve 1) [16—19].

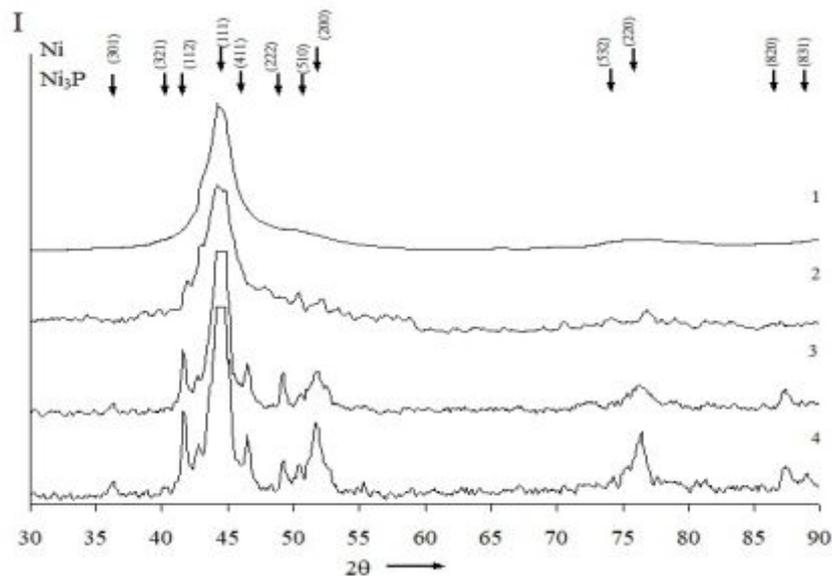


Fig. 1. Diffractograms of Ni-P alloys depending on pulse current regimes: 1 —  $\text{Ni}_{86}\text{P}_{14}$  ( $f=30$  Hz,  $Q=32$ ); 2 —  $\text{Ni}_{86}\text{P}_{14}$  ( $f=30$  Hz,  $Q=16$ ); 3 —  $\text{Ni}_{90}\text{P}_{10}$  ( $f=30$  Hz,  $Q=4$ ); 4 —  $\text{Ni}_{90}\text{P}_{10}$  ( $f=30$  Hz,  $Q=2$ ). Cu- $K_{\beta}$  radiation

Decreasing the pitch to 16 leads to a decrease in the potential growth rate to 120 V/s and, accordingly, to a decrease in the degree of imbalance of the obtained alloys. This contributes to the formation of a microcrystalline structure in the deposited alloys  $\text{Ni}_{86}\text{P}_{14}$ . On the diffractograms of alloys, diffraction maxima from lattices of crystalline fcc Ni and low-intensity lines from lattices of non-equilibrium phosphides appear against the background of diffuse maxima of the amorphous component  $\text{Ni}_5\text{P}_2$  and  $\text{Ni}_2\text{P}_{55}$ . A further decrease in the sparability to 4 leads to a decrease in the potential growth rate to 20 V/s, a decrease in the disequilibrium of the alloy deposition process and the phosphorus content in the film to 10 at. %, which contributes to the formation of a microcrystalline structure. On the diffractograms (Fig. 1, curves 3, 4) there are lines of microcrystalline Ni and phosphide  $\text{Ni}_3\text{P}$ . With a gap of 2, a decrease in the rate of potential growth to 7.5 V/s contributes to the formation of a crystal structure  $\text{Ni}_{90}\text{P}_{10}$ , which is indicated by clearer diffraction lines of the equilibrium phases of Ni and its phosphide  $\text{Ni}_3\text{P}$ . A similar picture of the dependence of the structure on pulsed current regimes is also characteristic of the Co-P alloy. As can be seen from fig. 2, curves 1—3, a decrease in the rate of potential growth from 154 to 5,4 V/s leads to a change in the formed structure from amorphous to a mixture of equilibrium crystalline phases b-Co and  $\text{Co}_2\text{P}$  (Fig. 2, curves 2 and 3). In the Fe-P alloy, as the potential growth rate decreases from 260 to 7,3 V/s, the amorphous structure changes to a mixture of crystalline b-Fe and amorphous  $\text{Fe}_3\text{P}$  (Fig. 3).

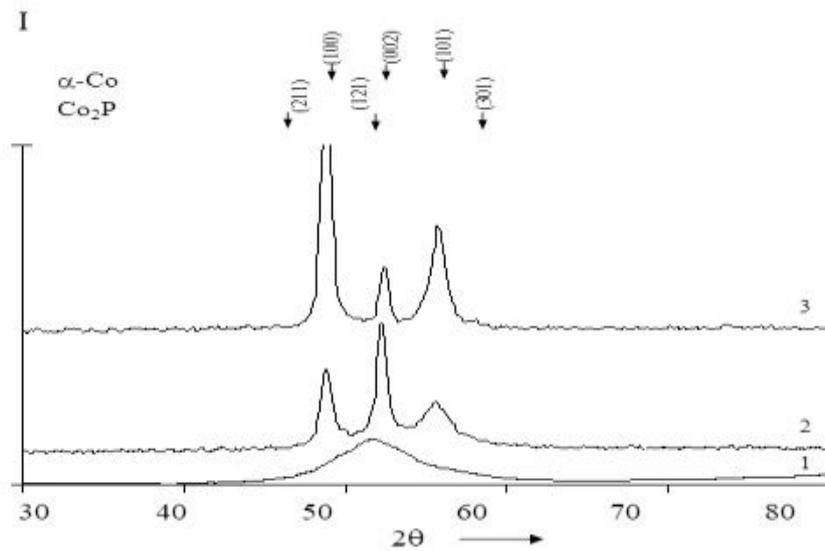


Fig. 2. Diffractograms of Co-P alloys depending on pulse current regimes: 1 —  $\text{Co}_{83}\text{P}_{17}$  ( $f=30$  Hz,  $Q=32$ ); 2 —  $\text{Co}_{83}\text{P}_{17}$  ( $f=30$  Hz,  $Q=16$ ); 3 —  $\text{Co}_{90}\text{P}_{10}$  ( $f=30$  Hz,  $Q=4$ ). Co- $K_b$  radiation

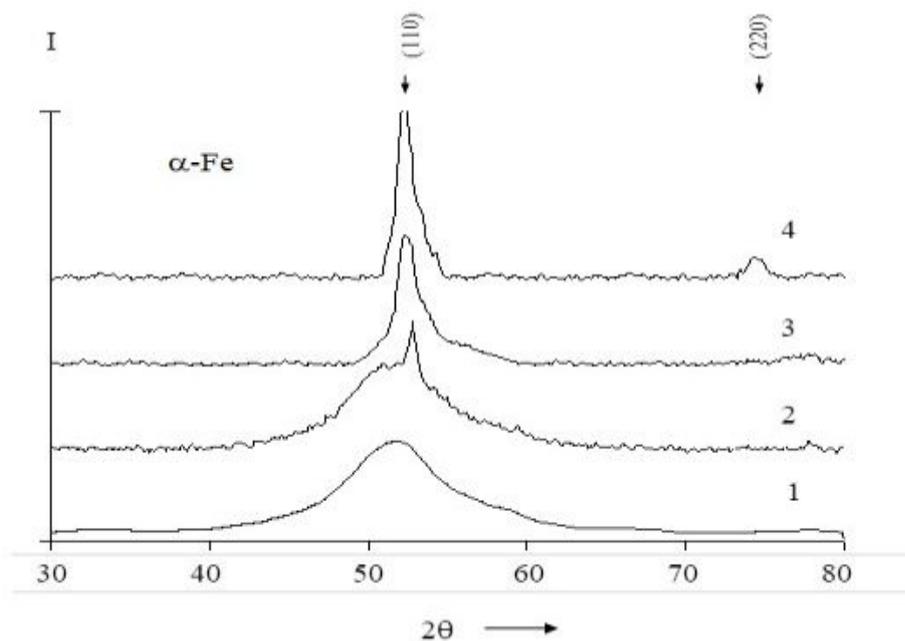


Fig. 3. Diffractograms of Fe-P alloys depending on pulse current regimes: 1 —  $\text{Fe}_{90}\text{P}_{10}$  ( $f=30$  Hz,  $Q=32$ ); 2 —  $\text{Fe}_{90}\text{P}_{10}$  ( $f=30$  Hz,  $Q=16$ ); 3 —  $\text{Fe}_{90}\text{P}_{10}$  ( $f=30$  Hz,  $Q=4$ ); 4 —  $\text{Fe}_{90}\text{P}_{10}$  ( $f=30$  Hz,  $Q=2$ ). Co- $K_b$  radiation

To clarify the phase state of the alloys, the microelectronograms of the alloys with the maximum phosphorus content were considered. Thus, in the  $\text{Ni}_{86}\text{P}_{14}$  alloy (Fig. 4), the width of the diffuse ring corresponds to the amorphous state with the dimensions of the OVRA up to 2 nm. Structure of alloys  $\text{Co}_{83}\text{P}_{17}$  (Fig. 5) and  $\text{Fe}_{83}\text{P}_{17}$  (Fig. 6) differs from amorphous because there are no continuous diffuse rings on microelectronograms. The presence of discontinuous rings with separate reflexes indicates that there are OVRAs larger than 2 nm in the volume, which can also be classified as amorphous, but with the presence of a more ordered composition [20].

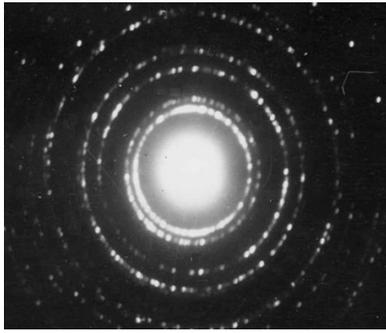


Fig. 4. Microelectronogram of the alloy  $\text{Ni}_{86}\text{P}_{14}$  (EMV-100L,  $U=75$  kВ).

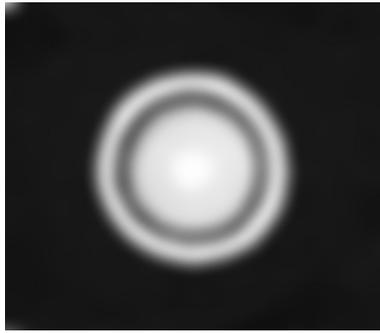


Fig. 5. Microelectronogram of the alloy  $\text{Co}_{83}\text{P}_{17}$  (EMV-100L,  $U=75$  kВ).

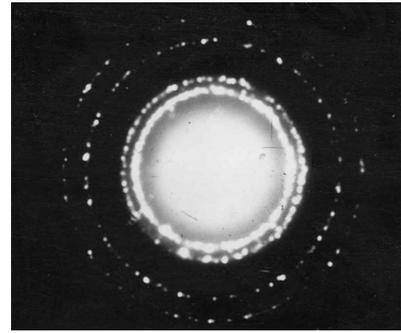


Fig. 6. Microelectronogram of the alloy  $\text{Fe}_{83}\text{P}_{17}$  (EMV-100L,  $U=75$  kВ).

The diffractograms of amorphous Co-P alloys, which were obtained using a pulsed current with a frequency of 30 Hz and a pitch of 32, show that they have three diffuse maxima each, similar to the typical diffractograms of amorphous PM-M alloys and have different degrees of amorphousness, which means that their close order has significant differences. As a result of experimental studies of the influence of deposition modes on the structure of alloys, it is shown that the formation of the amorphous state in Ni-P, Co-P, and Fe-P alloys is significantly influenced by the imbalance of the crystallization process during pulsed electrodeposition, which depends on the rate of increase of overvoltage on the cathode. It was also established that, in order to achieve an amorphous state in Ni-P, Co-P, and Fe-P alloys during pulsed electrodeposition, a 1—2 % lower phosphorus content is required, compared to alloys deposited using direct current.

### Conclusions

The study of the effect of cathodic overvoltage on the structure of electrodeposited Ni-P, Fe-P, and Co-P alloys was conducted, which showed the possibility of using a mathematical model of the dependence of the phase state of Ni-P, Co-P, and Fe-P alloys on pulsed current deposition modes.

### References

- [1] Skryshevsky A.F. (1980) Structural analysis of liquids and amorphous bodies. Moscow: Higher School.
- [2] Dutchak Y.I. (1977) Radiography of liquid metals. Lviv: Higher School.
- [3] Guinier A. (1961) X-ray crystals. Moscow: Fizmatgiz.
- [4] Mirkin L.I. (1961) Handbook of X-ray diffraction analysis of polycrystals. M.: Fiz.-mat. lit
- [5] Sadok J., Wagner H. (1986) Experiments on the diffraction of neutrons and x-rays on metallic glasses. Metal glasses: Atomic structure and dynamics, electronic structure, magnetic properties.
- [6] Cromer D.T., Mann J.B. (1968) X-ray scattering factors from numerical Hartree-Fock wave functions. *Acta Cryst.* vol 24.
- [7] Kostin N.A., Kublanovsky V.S., Zabludovsky V.A. (1989) Pulse electrolysis. Kyiv: Science thought.
- [8] Kostin N.A., Kublanovsky V.S. (1996) Pulse electrolysis of alloys. Kyiv: Science thought.
- [9] Gulivets O.M., Baskevich O.S., Zabludovsky V.O. (2004) Issledovanie vliyaniya katodnogo perenapryazheniya na strukturu elektroosazhennykh plenok Ni-P, Co-P [Study of the effect of cathodic overvoltage on the structure of electrodeposited Ni-P, Co-P membrans]. *Solid state physics and chemistry.* vol. 5, №. 3.
- [10] Gulivets A.N., Zabludovsky V.A., Baskevich A.S., Ganich R.F. (2005) Termicheckaya ustojchivost' i fazovye prevrashcheniya pri nagreve v splavah Fe-P, poluchennykh impul'snym elektrolizom [Thermal Stability and Phase Transformations on Heating in Fe-P Alloys Produced by Pulsed Electrolysis]. *FMM.* vol. 99, №. 5.
- [11] Zabludovsky V.A., Anishchenko T.I., Gulivets A.N., Shtapenko E.F. (2003) Vliyanie impul'snogo elektroliza na korrozionnyuyu stojkost' plenok So-P, Fe-P, Fe-Ni-P [Effect of pulsed electroly-

- sis on the corrosion resistance of Co-P, Fe-P, Fe-Ni-P membrans]. Kyiv. Proceedings of the 3rd International Scientific and Technical Conference "Surface Engineering and Product Renovation".
- [12] Gulivets A.N., Zabludovsky V.A., Shtapenko E.P., Kushnerev A.I., Dergachov M.P., Baskevich A.S. (2002) Mnogoslojnye sostavnye plenki Co-P s reguliruemymi magnitnymi svojstvami [Multilayer compound Co-P films with controlled magnetic properties]. *Transaction of the Institute of Metal Finishing*, vol. 80, № 5.
- [13] Petrov Y.N., Guryanov G.V., Bobanova Zh.I. and etc. (1990) Electrolytic deposition of iron. Chisinau: Shtiintsa.
- [14] Zabludovsky V.A. (1985) Uslovie obrazovaniya peresyshchennogo tverdogo rastvora vnedreniya vodoroda v nikelе pri impul'snom elektrolize [Condition for the formation of a supersaturated solid solution of hydrogen intercalation in nickel during pulsed electrolysis]. *Electrochemistry*, vol. 21, № 7.
- [15] Zabludovsky V.A., Shtapenko E.P., Gulivets A.N., Baskevich A.S., Ganitch R.P. (2001) Strukturnaya relaksaciya amorfnyh plenok Co-P, poluchennyh impul'snym tokom [The Structural Relaxation Of Amorphous Co-P Films Obtained By Pulsed Current]. *Transaction of the Institute of Metal Finishing*. vol. 79, № 6.
- [16] Lewis D.B., Marshall G.W. (1996) Issledovanie struktury gal'vanopokrytij nikel'-fosfornyh splavov [Investigation into the structure of electrodeposited nickel-phosphorous alloy deposits]. *Surface and Coatings Technology*, vol. 78.
- [17] Tarozaitė R., Kurtinaitienė M., Dziuvė A., Jusys Z. Sostav, mikrostruktura i magnitnye svojstva tonkih plenok Co-P, poluchennyh himicheskim osazhdeniem [Composition, microstructure and magnetic properties of electroless-plated thin Co-P films]. *Surface and Coatings Technology*, vol. 115.
- [18] Cebollada F. Gonzalez J.M., Julian C.de, Surinach S. (1997) Detal'nyj analiz kristallizacii amorfnoj sistemy Co-P: kinetika, vliyanie magnitnogo poryadka i formirovanie tekstur [Detailed analysis of the crystallization of the Co-P amorphous system: Kinetics, influence of magnetic order, and formation of textures]. *Physical Review*, vol 1, № 56(10).
- [19] Gadzyra N.F., Kharkov E.I. (1989) Ocenka doli kristallicheskoj fazy v metallicheskih steklah metodom rentgenovskogo analiza [Estimation of the fraction of the crystalline phase in metallic glasses by x-ray analysis]. *FMM*, vol. 68, no. 2.
- [20] B. Kantor (1983) Fast-hardened metals. Collection of scientific papers. Metallurgy.

### Список використаної літератури

1. Скрышевский А.Ф. Структурный анализ жидкостей и аморфных тел. М.: Высшая школа. 1980. 328 с.
2. Дутчак Я.И. Рентгенография жидких металлов. Львов: Вища школа. 1977. 163 с.
3. Гинье А. Рентгенография кристаллов. М.: Физматгиз, 1961. 604 с.
4. Миркин Л.И. Справочник по рентгеноструктурному анализу поликристаллов. М.: Физ.-мат. лит. 1961. 864 с.
5. Садоk Ж., Вагнер Х. Эксперименты по дифракции нейтронов и рентгеновских лучей на металлических стеклах. Металлические стекла: Вип. II. Атомная структура и динамика, электронная структура, магнитные свойства: Пер. с англ. / Под ред. Г. Бека и Г. Гюнтеродта. М.: Мир, 1986. 456 с.
6. Cromer D.T., Mann J.B. X-ray scattering factors from numerical Hartree-Fock wave functions *Acta Cryst.* 1968, A 24. P. 321-324.
7. Костин Н.А., Кублановский В.С., Заблудовский В.А., Импульсный электролиз. Киев: Наукова думка, 1989. 168 с.
8. Костин Н.А., Кублановский В.С. Импульсный электролиз сплавов. Киев: Наукова думка, 1996. 206 с.

9. Гулівець О.М., Дослідження впливу катодної перенапруги на структуру електроосаджених плівок Ni-P, Co-P / О.М. Гулівець, О.С. Баскевич, В.О. Заблудовський та ін. // Фізика і хімія твердого тіла. 2004. Т. 5, № 3. С. 572–576.
10. Гуливец А.Н. Термическая устойчивость и фазовые превращения при нагреве в сплавах Fe-P, полученных импульсным электролизом / А.Н. Гуливец, В.А. Заблудовский, А.С. Баскевич, Р.Ф. Ганич // ФММ. 2005. Т. 99, № 5. С. 62–65.
11. Заблудовский В.А. Влияние импульсного электролиза на коррозионную стойкость пленок Co-P, Fe-P, Fe-Ni-P / В.А. Заблудовский, Т.И. Анищенко, А.Н. Гуливец, Э.Ф. Штапенко и др. // Материалы 3-й Международной научно-технической конференции «Инженерия поверхности и реновация изделий». Киев. 2003. С. 65–66.
12. Gulivets A.N. Multilayer compound Co-P films with controlled magnetic properties / A.N. Gulivets, V.A. Zabudovsky, E.Ph. Shtapenko, A.I. Kushnerev, M.P. Dergachov, A.S. Baskevich // Transaction of the Institute of Metal Finishing. 2002. V.80, № 5. P. 154–156.
13. Петров Ю.Н. Электролитическое осаждение железа / Петров Ю.Н., Гурьянов Г.В., Бобанова Ж.И. и др. Кишинев.: Штиинца. 1990. 195 с.
14. Заблудовский В.А. Условие образования пересыщенного твердого раствора внедрения водорода в никеле при импульсном электролизе. Электрохимия. 1985. Т. 21, №. 7. С. 874–877.
15. Zabudovsky V.A. The Structural Relaxation Of Amorphous Co-P Films Obtained By Pulsed Current / V.A. Zabudovsky, E.Ph. Shtapenko, A.N. Gulivets, A.S. Baskevich, R.Ph. Ganitch // Transaction of the Institute of Metal Finishing. 2001. V. 79, № 6. P. 207–208.
16. Lewis D.B. Investigation into the structure of electrodeposited nickel-phosphorous alloy deposits / D.B. Lewis, G.W. Marshall // Surface and Coatings Technology. 1996. № 78. P. 150–156.
17. Tarozait R. Composition, microstructure and magnetic properties of electroless-plated thin Co-P films / R. Tarozait, M. Kurtinaitiene, A. Dziuve, Z. Jusys. // Surface and Coatings Technology. 1999, V.115. P. 57–65.
18. Cebollada F. Detailed analysis of the crystallization of the Co-P amorphous system: Kinetics, influence of magnetic order, and formation of textures / F.Cebollada, J.M.Gonzalez, C.de Julian, S.Surinach // Physical Review. 1997. B1, II, 56(10). P.6056–6065.
19. Гадзыра Н.Ф. Оценка доли кристаллической фазы в металлических стеклах методом рентгеновского анализа / Н.Ф. Гадзыра, Е.И. Харьков // ФММ. 1989. Т. 68, Вып. 2. С. 402–405.
20. Быстрозакаленные металлы / Сб. Науч.трудов. Под ред. Б Кантора. Пер. с англ. Под ред. А.Ф. Прокошина. М.: Металлургия. 1983. 472 с.

*Надійшла до редакції 20.03.2023*